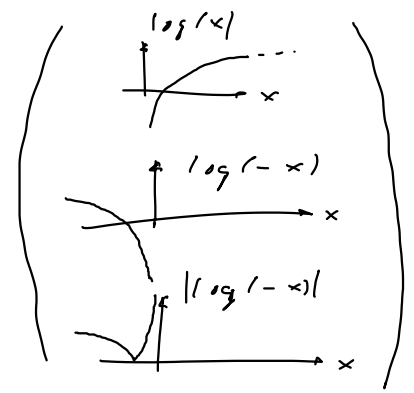
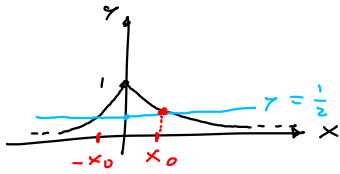


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$$f(x) = e^{-2|x|} \quad ; \quad g(x) = |\log(-x)|$$

(i)



(ii)  $f(x) + 2 > \frac{5}{2}$

$$f(x) > \frac{1}{2}$$

$$e^{-2|x_0|} = \frac{1}{2}$$

i.e.  $e^{-2x_0} = \frac{1}{2} \quad / \log(\dots)$

$$\begin{aligned} -2x_0 &= \log\left(\frac{1}{2}\right) \\ \rightarrow x_0 &= -\frac{\log\left(\frac{1}{2}\right)}{2} = -\frac{\log(2^{-1})}{2} = \frac{\log(2)}{2} \end{aligned}$$

$$\rightarrow \underline{\underline{L = \left(-\frac{\log(2)}{2}, \frac{\log(2)}{2}\right)}}$$

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$$\frac{n}{k} \cdot \frac{(n-1)!}{(n-1-(k-1))! (k-1)!} = \frac{n!}{k (n-k)! (k-1)!} = \frac{n!}{(n-k)! k!} = \binom{n}{k}$$

$$\binom{n}{k} = \frac{n!}{(n-k)! k!}$$

$$\left( n(n-1)! = \underbrace{n \cdot 1 \cdot 2 \cdot 3 \cdot 4 \cdot 5 \cdot \dots \cdot (n-2)(n-1)}_{(n-1)!} = n! \right)$$

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(iv)  $\lim_{x \rightarrow 0} \frac{\sqrt{1+x} - 1}{x} = \lim_{x \rightarrow 0} \frac{(\sqrt{1+x} - 1)}{x} \quad [\text{siehe VL 9.11.20}]$

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(iv)  $\lim_{t \rightarrow -1} \frac{t^2 + 3t + 2}{t^2 - t - 2} = \lim_{t \rightarrow -1} \frac{(t+2)(t+1)}{(t+1)(t-2)} = \lim_{t \rightarrow -1} \frac{t+2}{t-2} = \underline{\underline{-\frac{1}{3}}}$